

**Abstract** We show that, for each orientable surface  $\Sigma$ , there is a constant  $c_\Sigma$  so that, if  $G_1$  and  $G_2$  are embedded simultaneously in the orientable surface  $\Sigma$ , with representativities  $r_1$  and  $r_2$ , respectively, then the minimum number  $cr(G_1, G_2)$  of crossings between the two maps satisfies

$$cr(G_1, G_2) \leq \frac{c_\Sigma}{r_1 r_2} |E(G_1)| |E(G_2)| .$$

This refines earlier estimates by Negami. Furthermore, we provide a counterexample to a conjecture of Archdeacon and Bonnington by exhibiting, for each  $k$ , embeddings  $G_1$  and  $G_2$  in the double torus so that, if we force all the vertices of  $G_1$  to be in the same face of  $G_2$ , then the number of crossings between  $G_1$  and  $G_2$  is at least  $k \cdot cr(G_1, G_2)$ .